

# The Market Value of Wind and Solar Power: an Analytical Approach

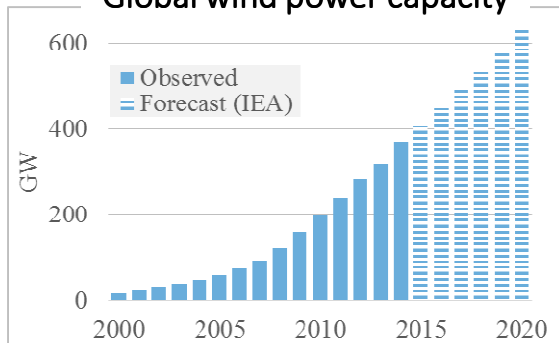
Lion Hirth & Alexander Radebach

Strommarkttreffen | 27 November 2015 | [hirth@neon-energie.de](mailto:hirth@neon-energie.de)

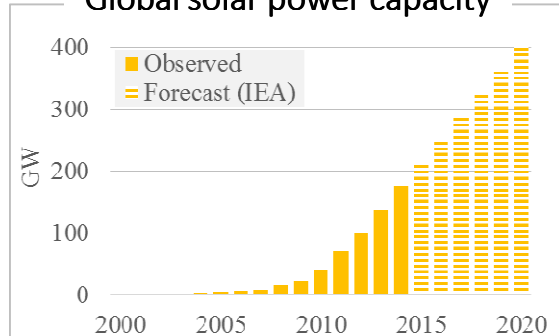
This is work in progress

# Wind & sun deliver 15+% of electricity in some regions

## Global wind power capacity



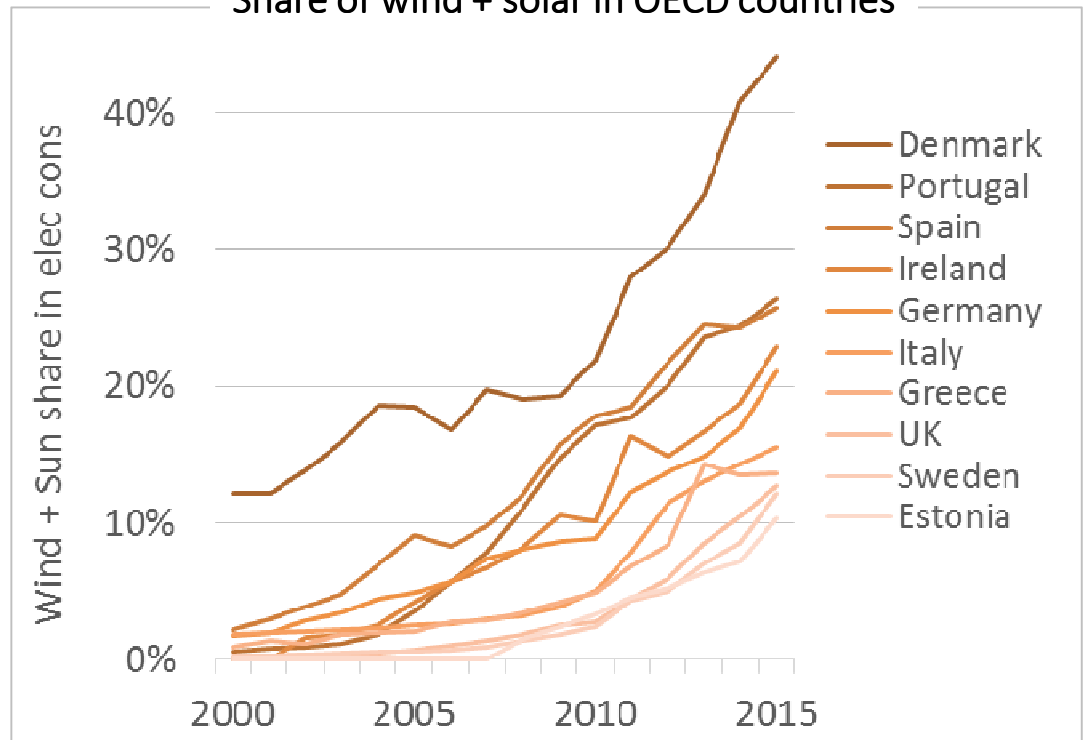
## Global solar power capacity



Data source: REN21 (2015), IEA (2014)

Wind and solar power have been growing strongly, and are expected to continue to grow.

## Share of wind + solar in OECD countries

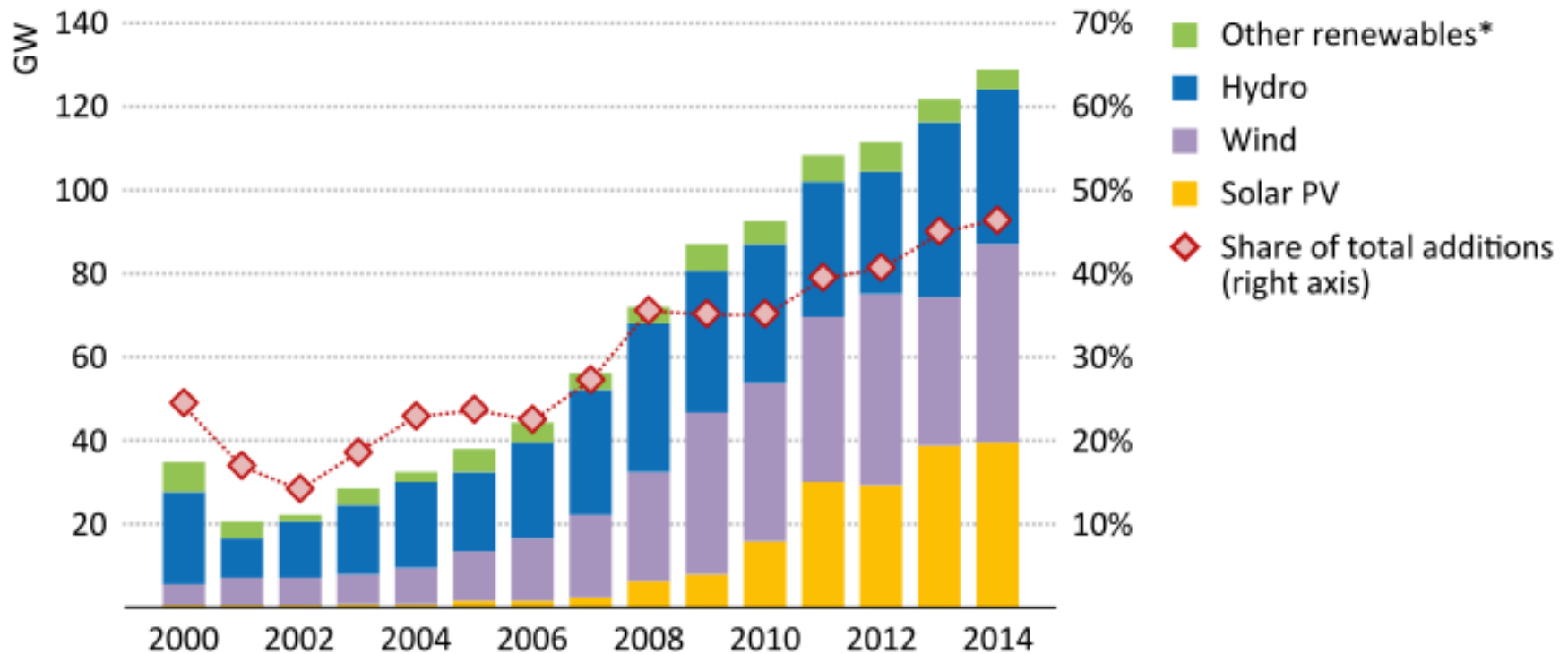


Data source: IEA (2015)

Wind and solar power combined now supply more than 10% of electricity in several power systems (and more than 20% in some) – they have become mainstream technologies.

# 50% of globally added capacity is renewable

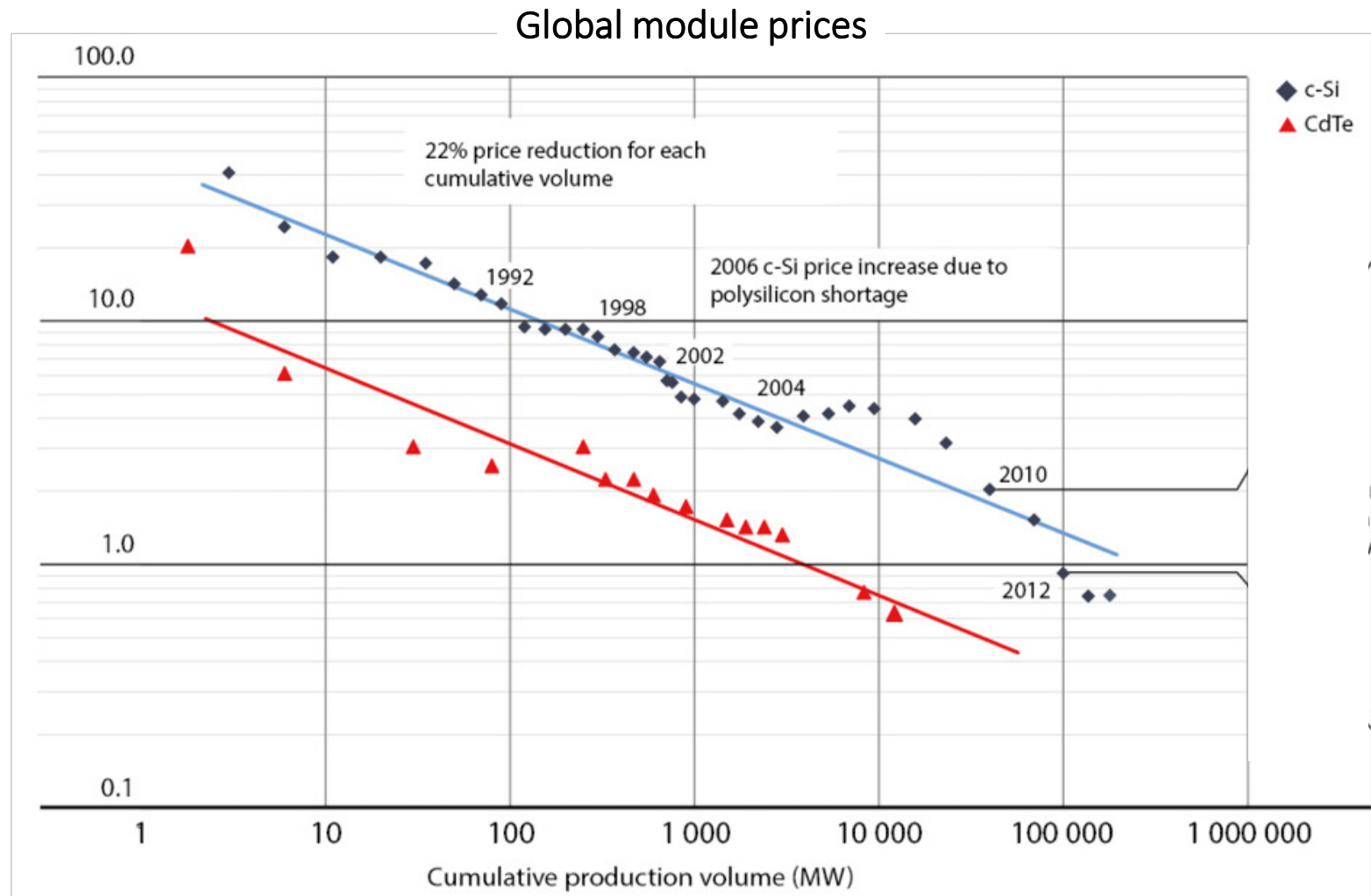
Global power generation additions



Source: IEA (2015): WEO special report

In 2014, almost half of all new power generation capacity globally was based on renewables – of which wind and solar power captured the lion's share of 70%.

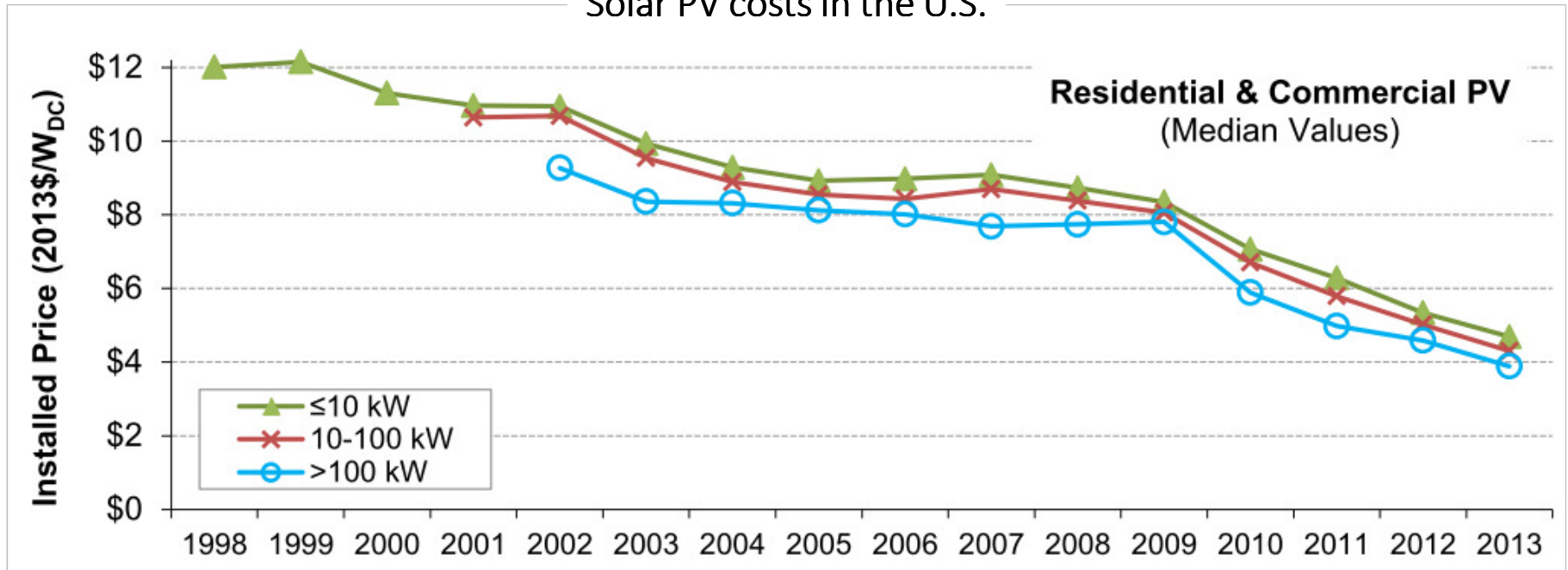
# Renewables are becoming cheaper and cheaper ...



LBNL (2014): Tracking the Sun VII

# Renewables are becoming cheaper and cheaper ...

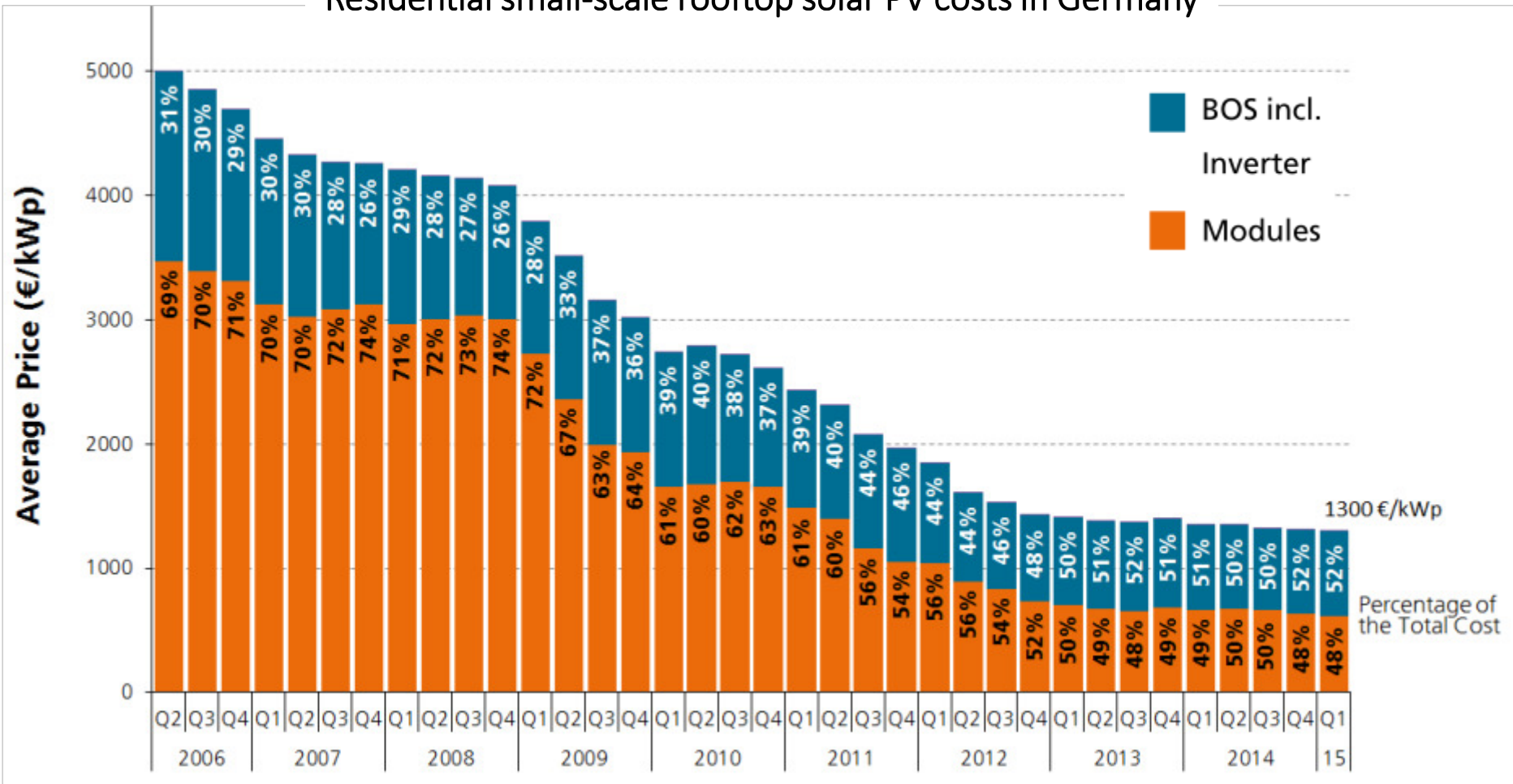
Solar PV costs in the U.S.



LBNL (2014): Tracking the Sun VII

# Renewables are becoming cheaper and cheaper ...

Residential small-scale rooftop solar PV costs in Germany

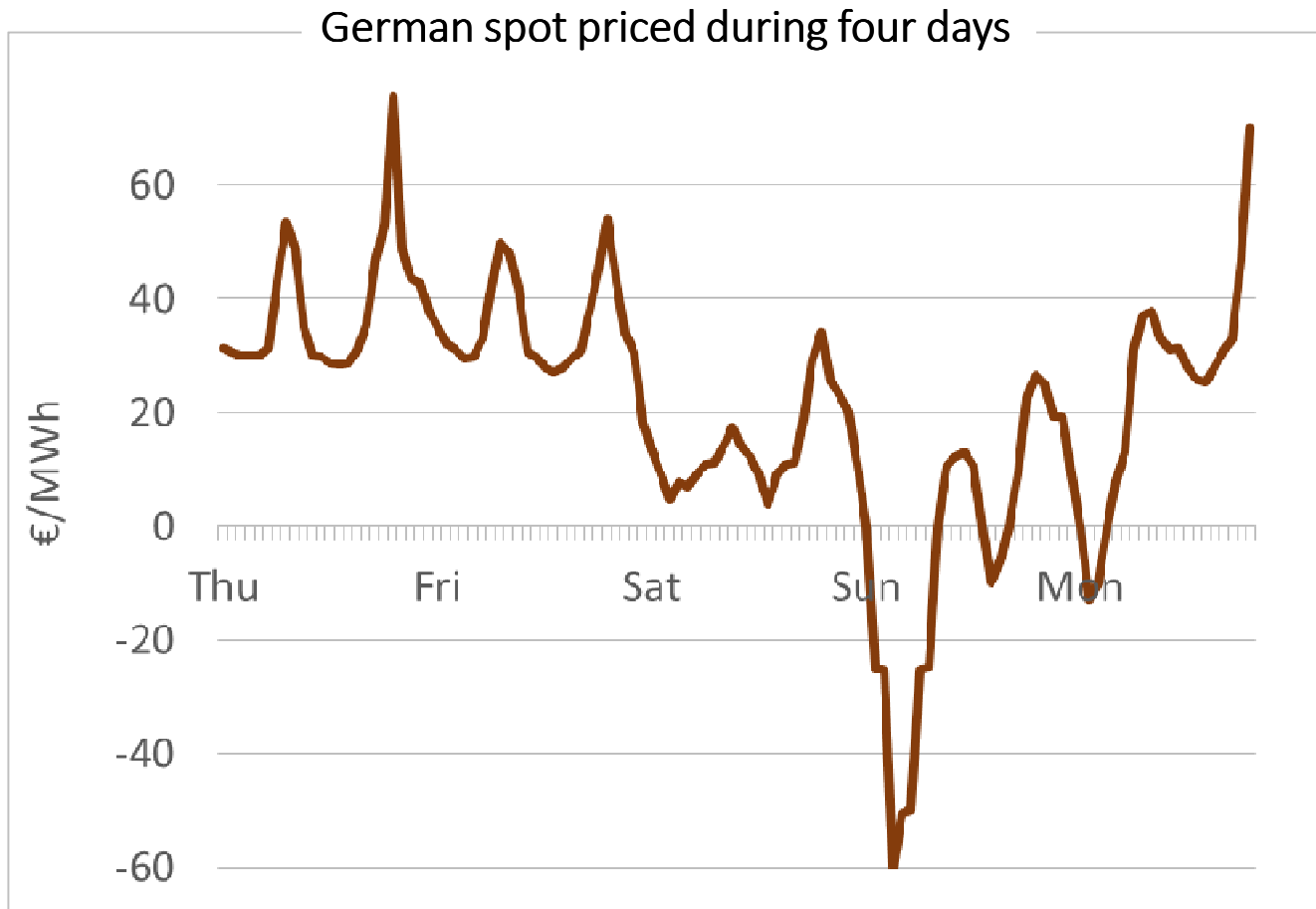


Source: Fraunhofer ISE (2015): Photovoltaics Report

Economics has two sides:  
costs and *value*



For economics, it matters *when* electricity is produced



German day-ahead spot price. 13-17 March 2014. On Sunday morning, the instantaneous wind penetration rate exceeded 50%.

# Value factor: the relative price of wind power

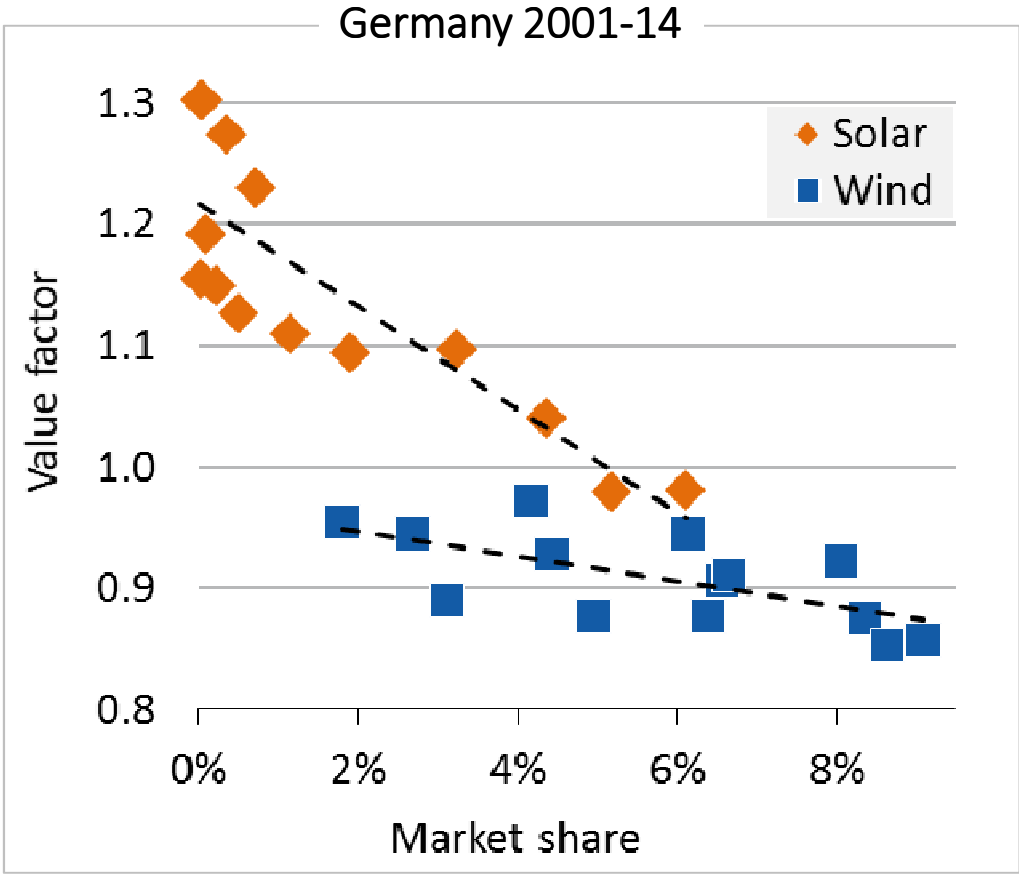
Wind in Germany			
	Base price (€/MWh)	Wind Revenue (€/MWh)	Value Factor (1)
2001	23.1	22.7	0.96
...	...	...	...
2014	35	30	.86

↑  
Simple  
average  
of all hours  
of the year

↑  
Wind-  
weighted  
average

↑  
Ratio of  
these two

# The wind and solar value drop



Value Factor =  
Market value /  
base price

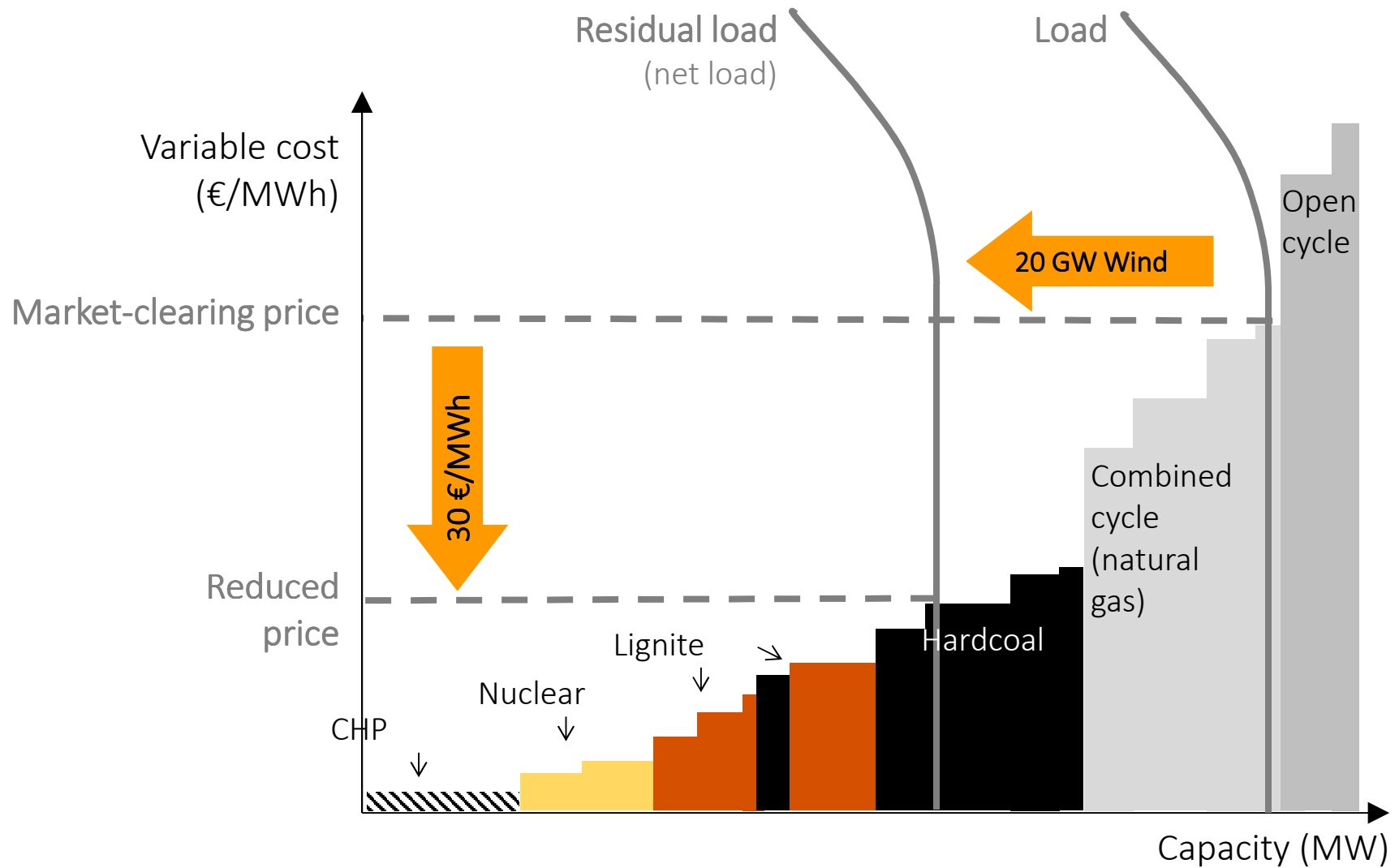
Each dot represents  
one year



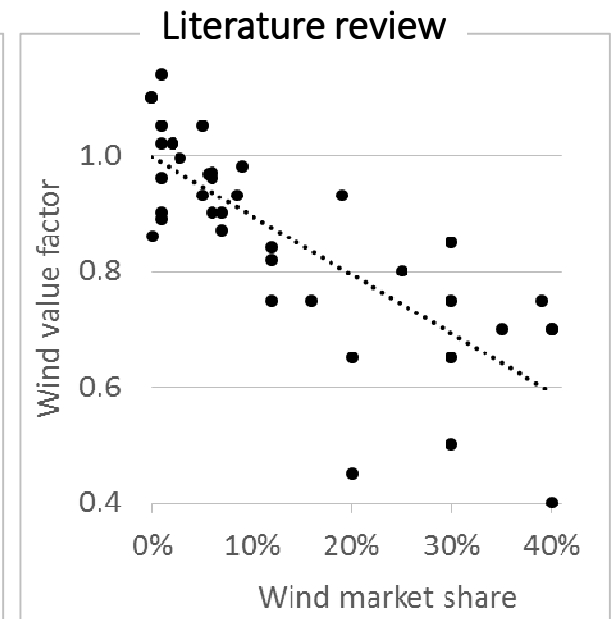
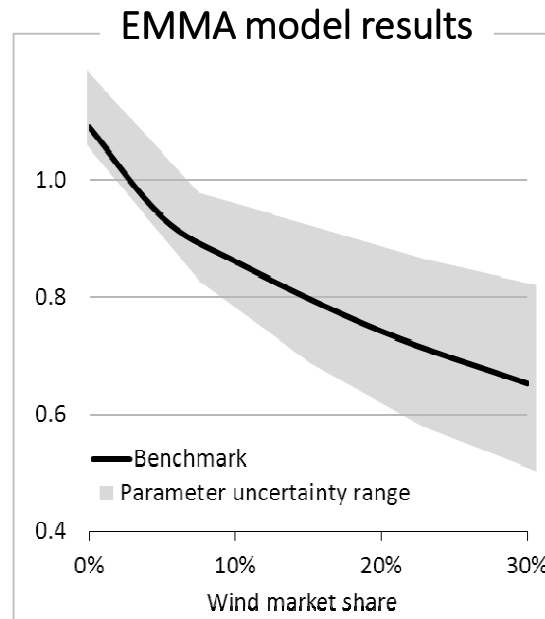
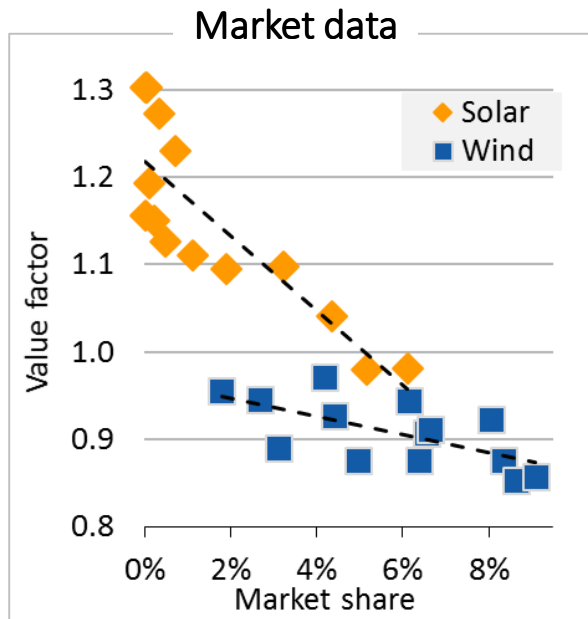
Updated from Hirth (2013).: Market value

The relative value of electricity from wind and solar power is reduced as their market share grows. This has been called the “cannibalization effect”, but in fact it is simply diminishing returns. For solar power, the value drop is more pronounced.

# The mechanics behind the value drop



# Different methodologies – robust finding: value drops



Updated from Hirth (2013): Market value and Hirth (2015): Market value solar

At 30% penetration, the value factor of wind falls to 0.5 – 0.8 of the base price. In Germany, it has already fallen from 0.96 to 0.86 as penetration increased from 2% to 8%. The value drop jeopardizes power system decarbonization and transformation.

# Market value research

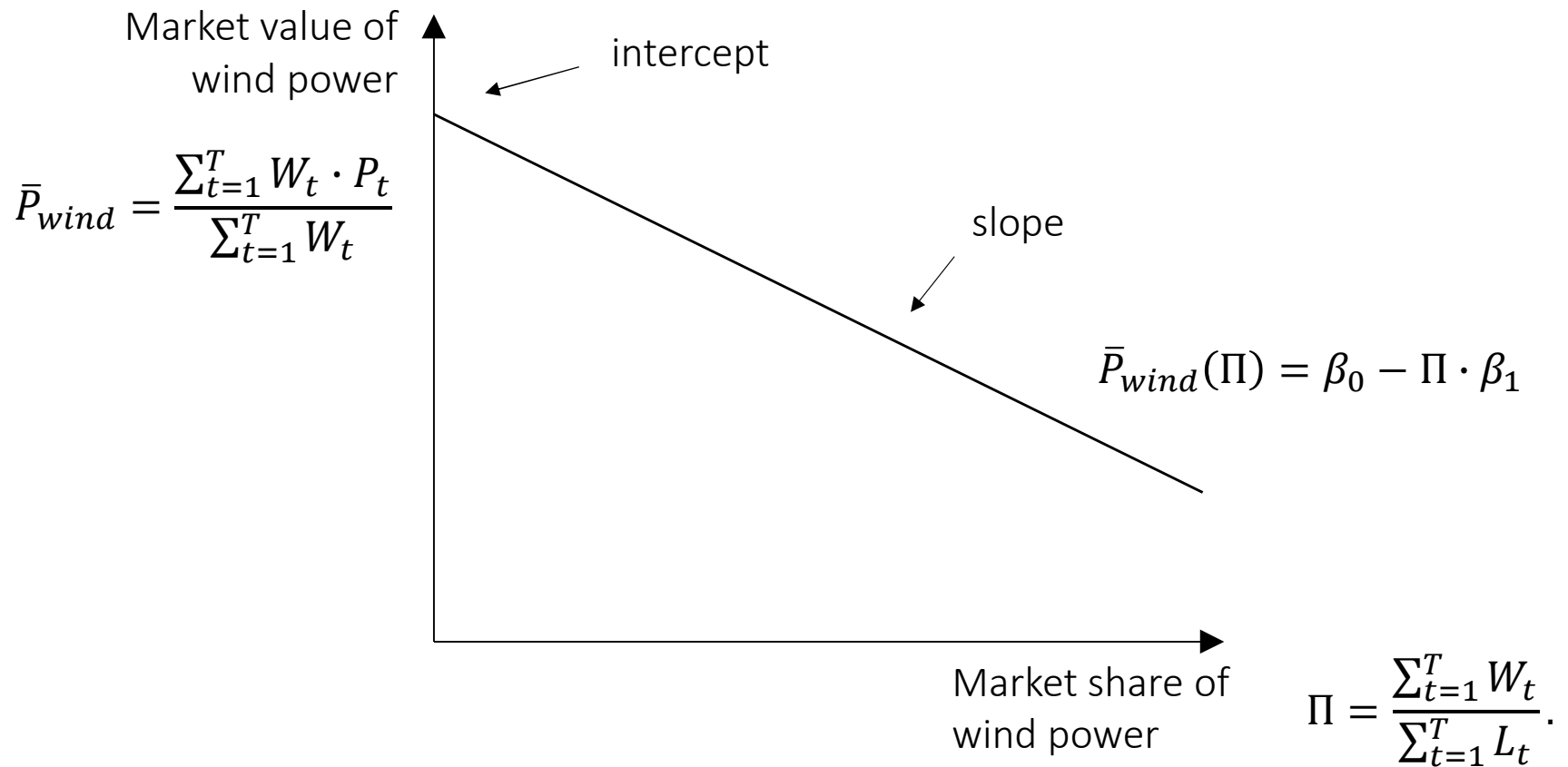
## Status quo of the literature

- Many quantitative studies based on numerical modelling
- Scatter literature, lack of synthesis
- Little theoretical understanding, in fact, Lamont (2008) might be the only one

## Our contributions to the literature

1. Empirical: new data, new econometrics, better synthesis
2. Theoretical: an analytical expression for the value drop

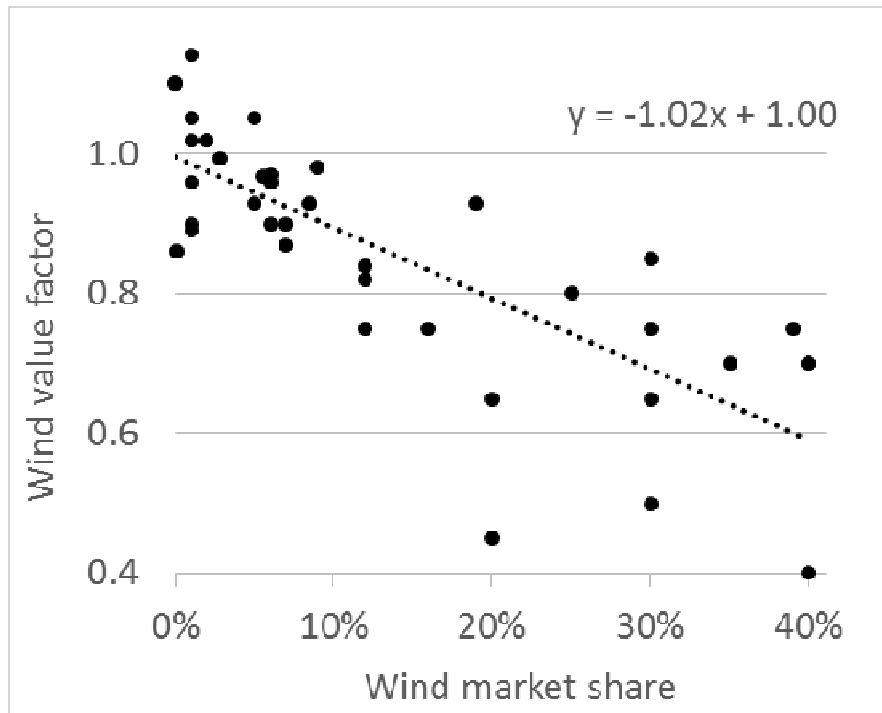
# A (linear) approximation of the value drop



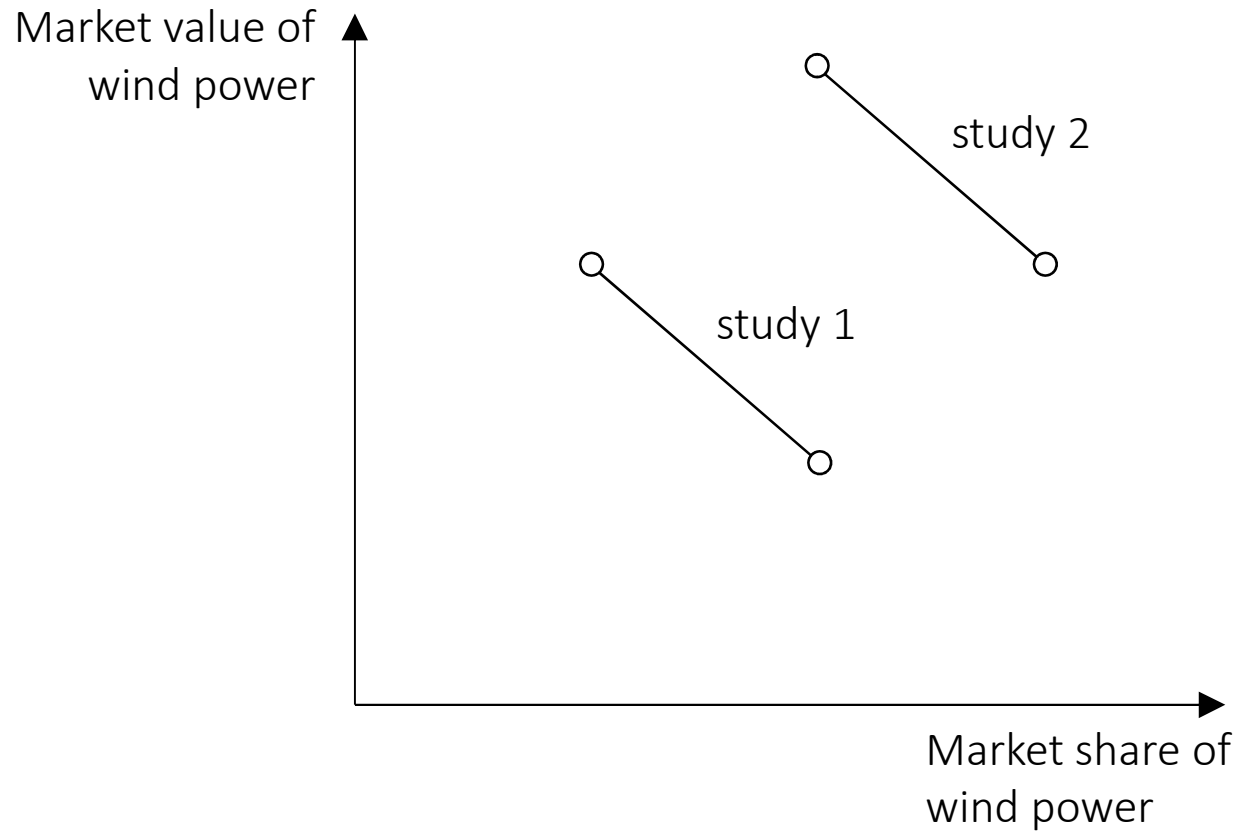
# 1. Econometrics



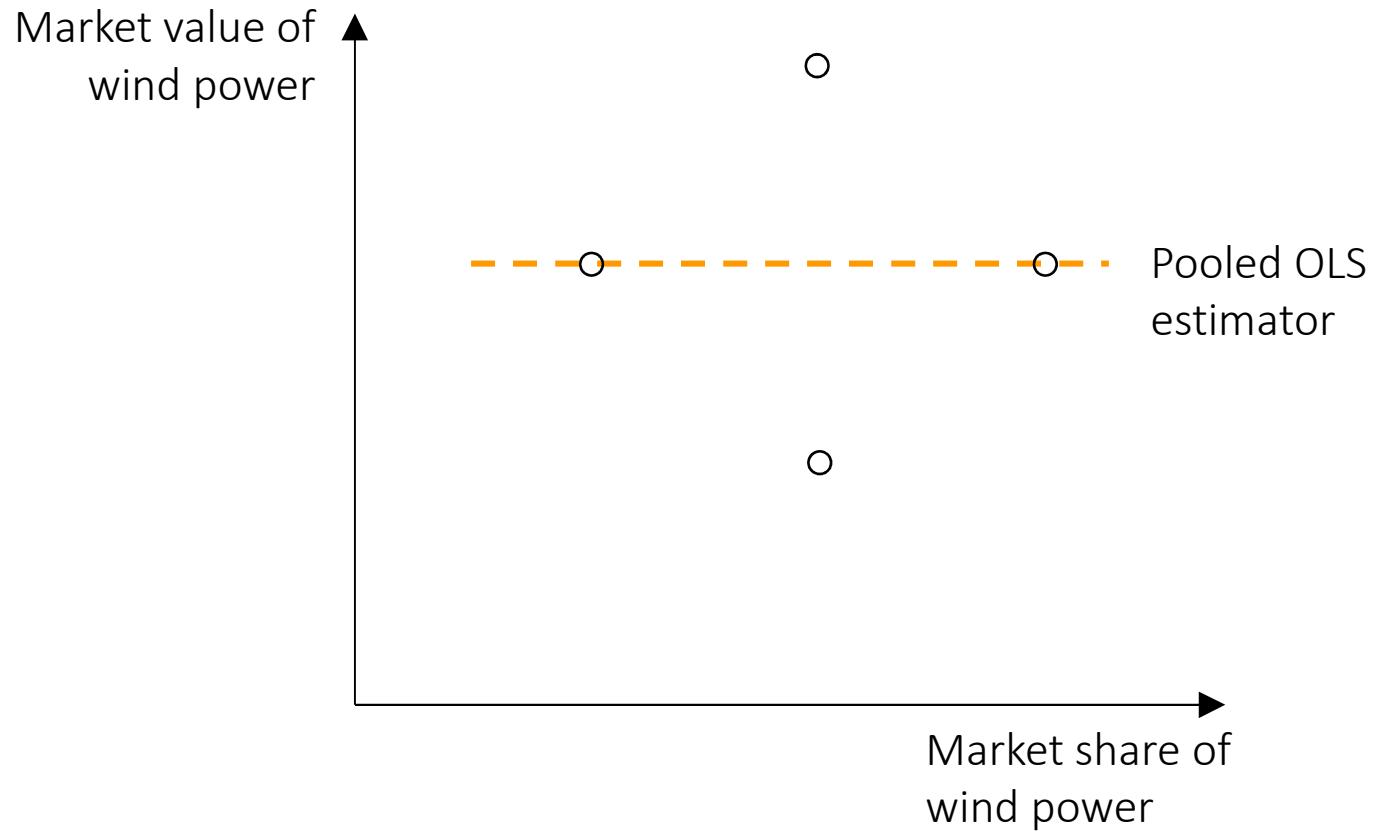
# Quantitative Literature: overview



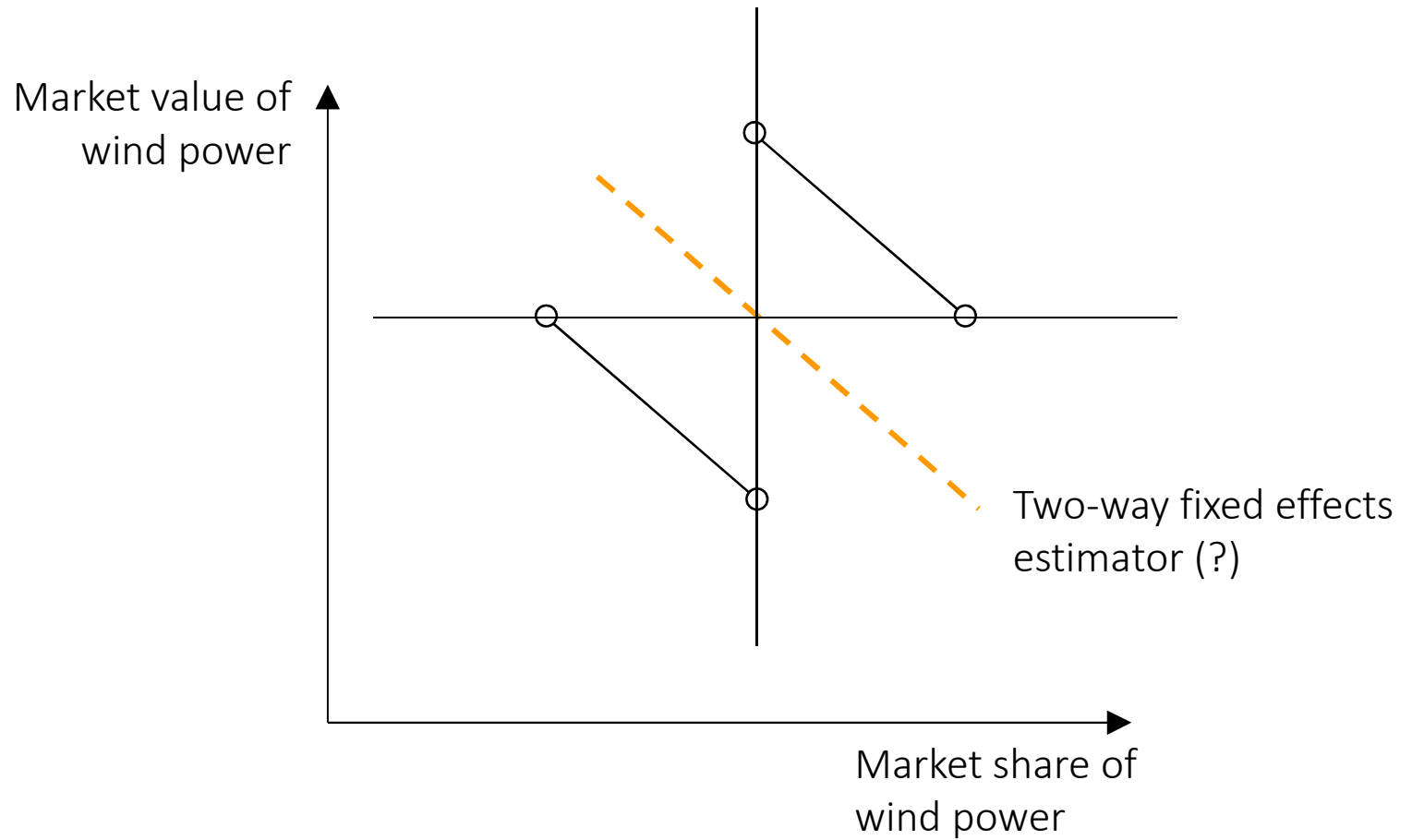
# Within- and between study variation



# Within- and between study variation



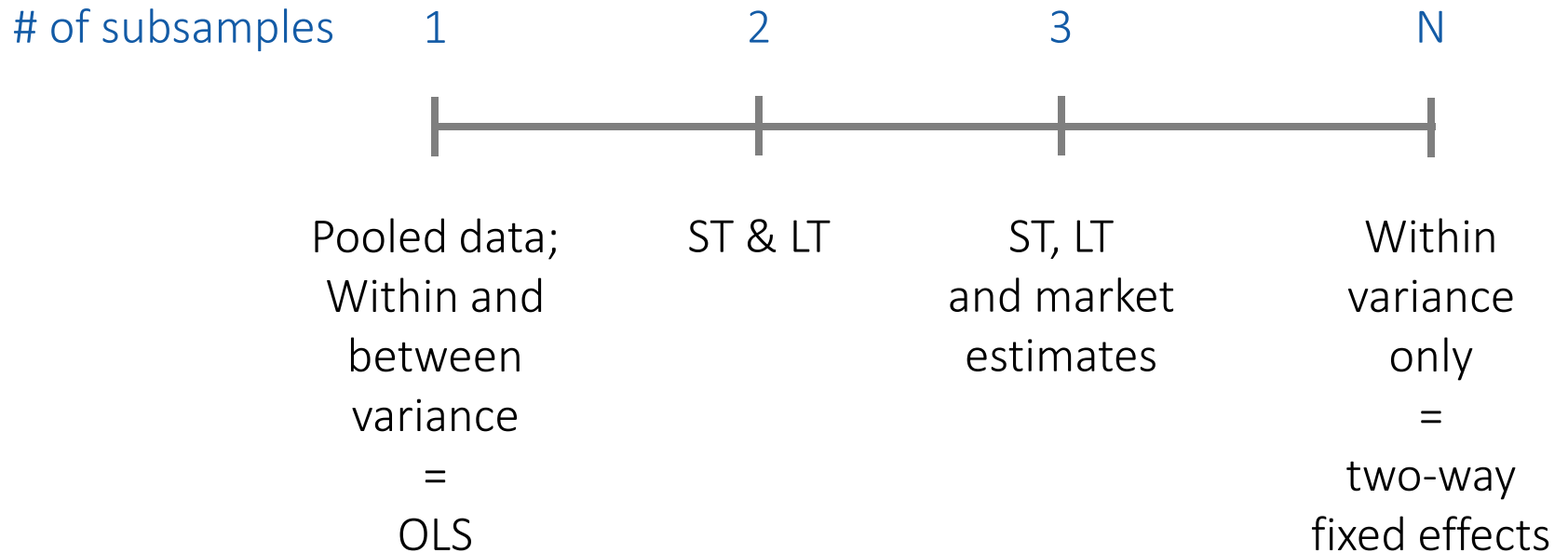
# Within- and between study variation

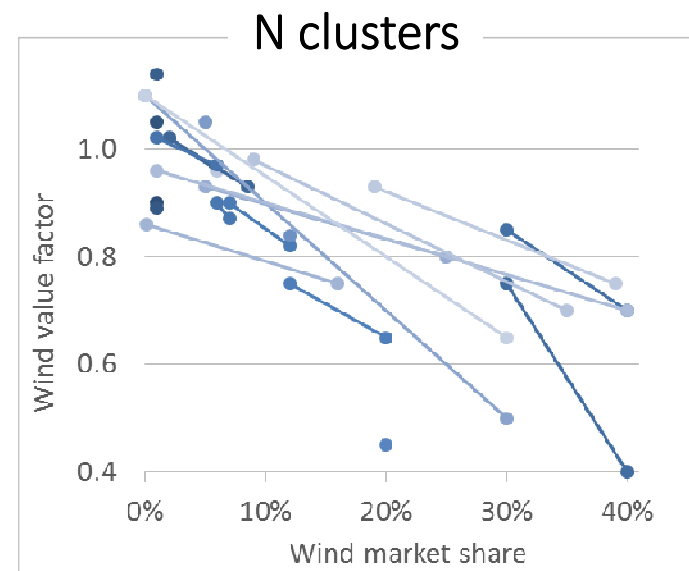
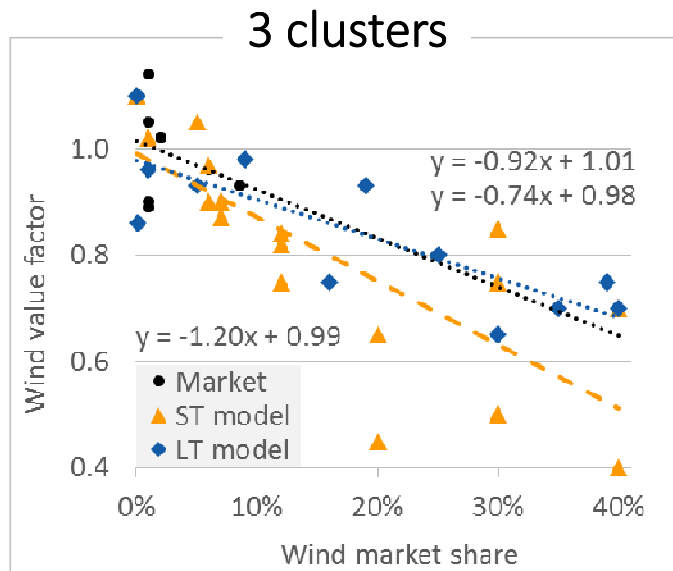
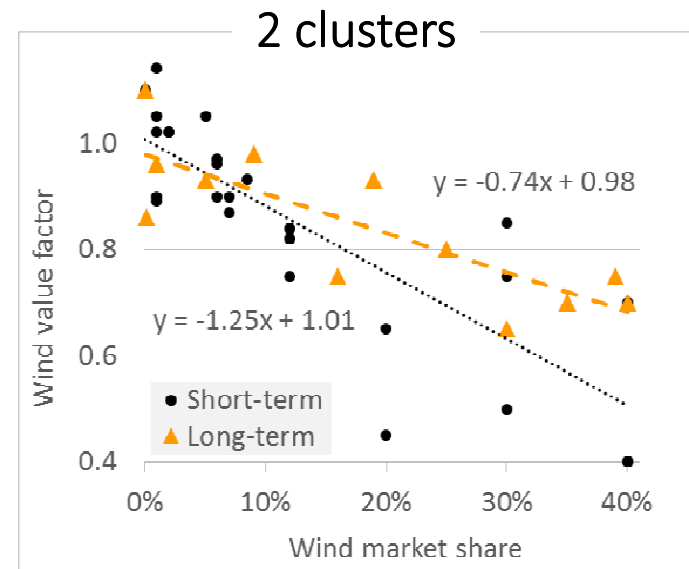
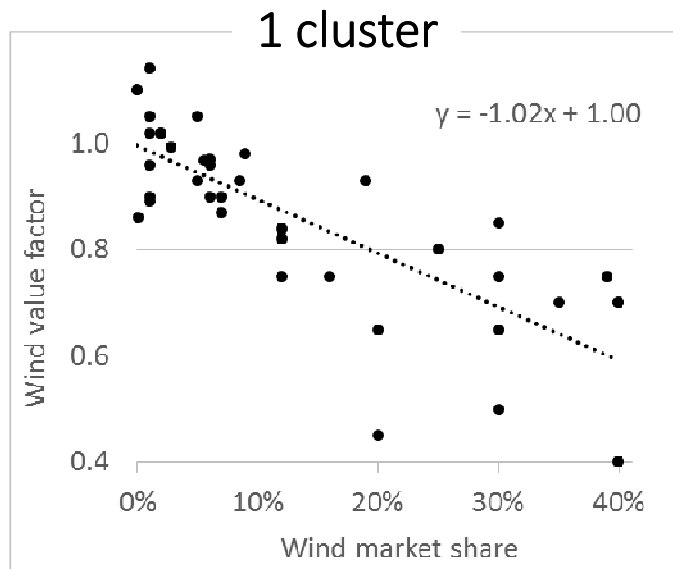


# Clustering based on exogenous information

- We know not only results, also methodology of studies
- We can cluster studies into two groups
  - short-term approaches (ST)
  - long-term approaches (LT)
  - expectation: slope should be smaller in LT models, as they account for capital adjustments
- We can also cluster studies into three groups
  - short-term approaches based on numerical modelling (ST models)
  - econometric estimates based on observed market data (market)
  - long-term approaches based on numerical modelling (LT models)

# Clustering estimates





# Clustering and pooling

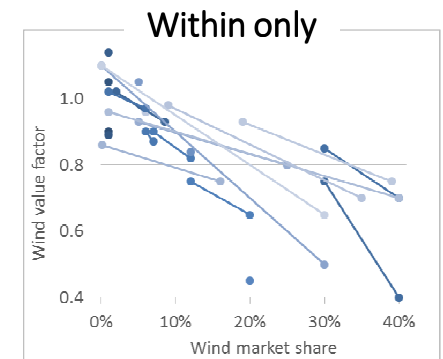
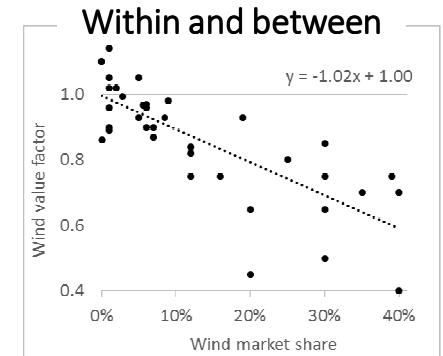
	1 cluster	2 clusters	3 clusters	N clusters
Pooled (OLS)	x	x	x	x
Separated (2-way fixed effects)	x	x	x	-

For separate model, we report mean coefficient estimates (model democracy, or rather: “study democracy”).



# Results: different estimates

<i>Slope estimate</i>	# of studies	OLS (within & between)	FE (within only)
Pooled	18	-1.0	-1.5
Short-term	12	-1.3	-1.9
Long-term	16	-0.7	-0.9
Market data	4	-0.9	-1.4
Short-term model	8	-1.2	-2.0
Long-term model	6	-0.7	-0.9



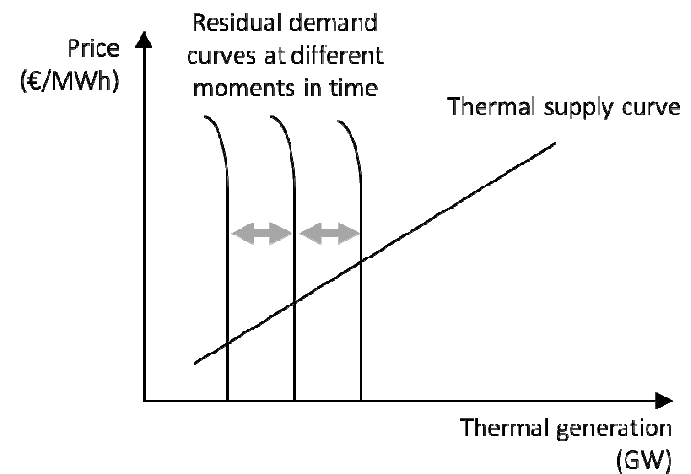
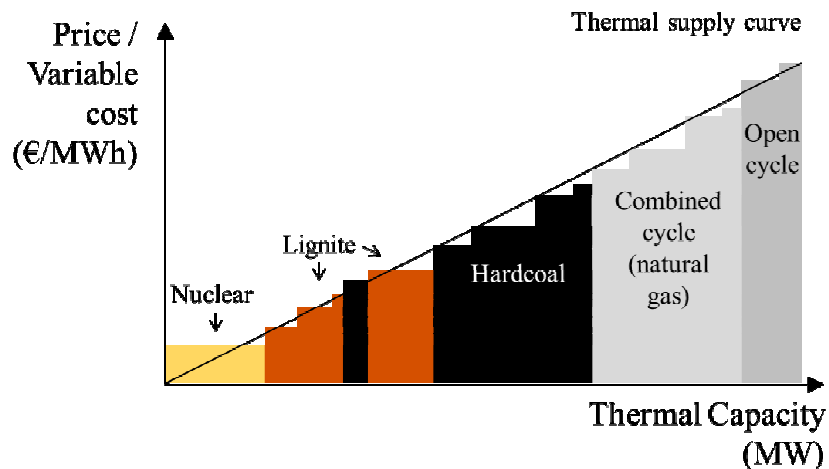
- Short-term numerical models estimate steeper slope than market data suggests
- Studies Individually show steeper slope than pooled sample.

# Conclusions and next steps

- New studies and more diverse econometric approaches confirm the established result: the value factor (relative price) of wind power drops as its market share increases
- Long-term models (accounting for changes in the capacity mix): drop of 0.7 – 0.9 percentage points per percentage point increase in market share
- Short-term models and market data estimates: 0.9 – 2.0
- What is the information value of between-model variation?
- Apply panel data techniques more rigorously?

## 2. Theory

# A linearized supply curve (merit-order curve)



$$P_t = \alpha \cdot \frac{R_t}{L_{max}}$$

$$R_t = L_t - W_t$$

# The market value of wind power: analytically

- $P_t = \alpha \cdot \frac{R_t}{L_{max}}$  (price, as above)
- $\lambda_t = \frac{L_t}{L_{max}}$  (normalized load time series)
- $\omega_t = \frac{W_t}{C}$  (normalized wind in-feed time series)
- $\bar{P}_{wind} = \frac{\alpha}{L_{max}} \cdot \frac{\sum_{t=1}^T W_t \cdot R_t}{\sum_{t=1}^T W_t}$  (market value definition, as above)
- $\bar{P}_{wind} = \frac{\alpha}{L_{max}} \cdot \left\{ L_{max} \cdot \frac{\sum_{t=1}^T \omega_t \cdot \lambda_t}{\sum_{t=1}^T \omega_t} - C \cdot \frac{\sum_{t=1}^T \omega_t^2}{\sum_{t=1}^T \omega_t} \right\}$
- $C = \Pi \frac{\bar{L}}{\bar{\omega}} = \Pi \frac{\bar{\lambda} \cdot L_{max}}{\bar{\omega}}$
- $\bar{P}_{wind} = \alpha \cdot \left\{ \frac{\sum_{t=1}^T \omega_t \cdot \lambda_t}{\sum_{t=1}^T \omega_t} - \Pi \cdot \frac{\bar{\lambda}}{\bar{\omega}} \cdot \frac{\sum_{t=1}^T \omega_t^2}{\sum_{t=1}^T \omega_t} \right\}$

# Market value in terms of (co-) variances

Using the fact that:

- $cov(\omega_t, \lambda_t) = \frac{1}{T} \sum_{t=1}^T \omega_t \cdot \lambda_t - \bar{\omega} \bar{\lambda}$  (definition of covariance)
- $var(\omega_t) = \frac{1}{T} \sum_{t=1}^T \omega_t^2 - \bar{\omega}^2$  (definition of variance)
- $c_v(\omega_t) = \frac{\sqrt{var(\omega_t)}}{\bar{\omega}}$  (def. of coefficient of variation)

We derive:

- $\bar{P}_{wind} = \alpha \cdot \bar{\lambda} \cdot \left\{ \left( 1 + \frac{cov(\omega_t, \lambda_t)}{\bar{\lambda} \bar{\omega}} \right) - \Pi \cdot \left( 1 + \frac{var(\omega_t)}{\bar{\omega}^2} \right) \right\}$
- $\bar{P}_{wind} = \alpha \cdot \bar{\lambda} \cdot \left\{ \left( 1 + \frac{cov(\omega_t, \lambda_t)}{\bar{\lambda} \bar{\omega}} \right) - \Pi \cdot (1 + c_v(\omega_t)^2) \right\}$

# Interpreting: intercept and slope

$$\bar{P}_{wind} = \alpha \cdot \bar{\lambda} \cdot \left\{ \left( 1 + \frac{cov(\omega_t, \lambda_t)}{\bar{\lambda}\bar{\omega}} \right) - \Pi \cdot (1 + c_v(\omega_t)^2) \right\}$$

*Intercept: a function of ...*

*Slope: a function of ...*

$$\lim_{\Pi \rightarrow 0} \bar{P}_{wind} = \bar{P} \cdot \left( 1 + \frac{cov(\omega_t, \lambda_t)}{\bar{\lambda}\bar{\omega}} \right)$$

$$\frac{\partial \bar{P}_{wind}}{\partial \Pi} = -\alpha \cdot \bar{\lambda} \cdot (1 + c_v(\omega_t)^2)$$

- ... the covariance btw load & wind
- ... the “capacity factors “ of both time series

- ... the capacity factor of load
- ... the variance of wind generation, expressed as it’s coefficient of variation

Wind	Solar
1.02	1.05

Wind	Solar
-1.25	-2.47

# Conclusions and next steps

- To the best of our knowledge, this is the first expression of the market value of wind power as a function of its statistical properties and those of load
- Lamont (2008) provides the only other expression, but assumes prices to be given
- It is the covariance between load and wind that determines the wind value initially
- *It is the variance of wind that determines the value drop* – independent of the correlation with load
- Constant wind generation would also lead to dropping value, but the slowest drop possible
- “More constant” wind generation is more robust against value loss: wind turbines with a higher capacity factor and lower coefficient of variation  
→ Hirth & Müller (forthcoming)



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